# From Stories to Concurrency: How Children Can Play with Formal Methods

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### Citation from a Review

From one of the reviews of yesterday's paper:

What struck me as a surprise was the authors' promotion of teaching formal methods even to school children in some form.

Misconception that mathematics and computer science are two independent, fully distinct disciplines

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Misconception that mathematics and computer science are two independent, fully distinct disciplines  $\longleftarrow$ 

- computer science is identified with programming and use of computers
- programming is is seen as an art rather than a science
- ⇒ Belief that computer science does not require mathematical skills
  ⇒ gap between computer science and mathematics

### Computer Science in Schools

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Computers have been heavily introduced in schools and in many schools computer science is taught as a new, stand-alone subject, but it is seen

- as a "service subject" to provide tools that facilitate students in carrying out their homework and class projects, and are supposed to enhance their learning
- as intrinsically tied to the use of computers

### Formal Methods for Children

Formal methods fill in the gap between computer science and mathematics

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discovery concepts and internalisation

informally/visually

with fun

analysis

(visual notations)

school pupils

problem maths solving

interdisciplinary context

other subjects unplugged approach

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#### **Primary School**

intrinsic motivations (fun, challenge, competition)

Intermediate and High School extrinsic motivations

maths

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**Primary School** 

intrinsic motivations (fun, challenge, competition)

Intermediate and High School extrinsic motivations

parallel stories

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choose your own adventure

unplugged approach

Concept created by Edward Packard First book of the series in 1976

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#### Children

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### Because ...

# Children are very interested in complex systems acted by many processes, who

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- interact and synchronise on specific situations
- cooperate to solve problems, and
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#### Children

- can make sense of the composition of individual processes and
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### Question on the Story

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- Which are your possible choices?
- Which choice would you make?
- Do you know which door lead to the treasure and which to death?

Your friend is also looking for the treasure. You both start at the same time but following different paths and getting to the castle at different times. Your friend understands only the parrot on the right of the large door. The other parrot speaks a language unknown to your friend.

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#### Questions:

• Is the key needed to reach the treasure?

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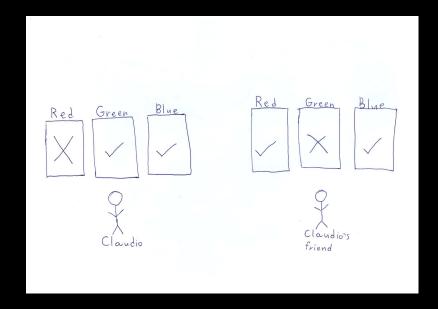
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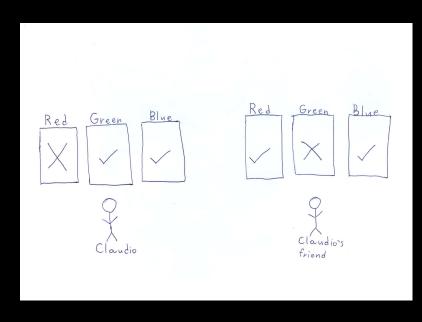
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- Which door leads to the treasure?
- Can you be sure that you reach the treasure without dying?

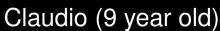
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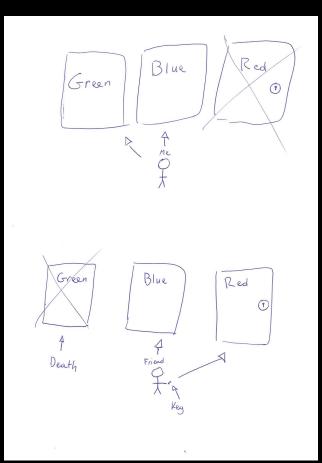
- Is the key needed to reach the treasure?
- Which door leads to the treasure?
- Can you be sure that you reach the treasure without dying? Collaboration



Claudio (9 year old)

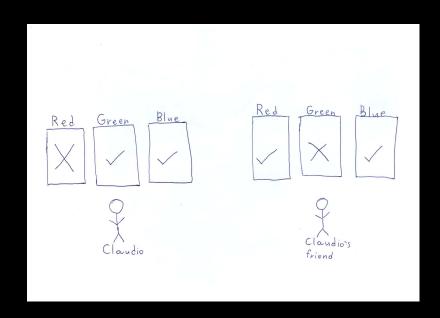




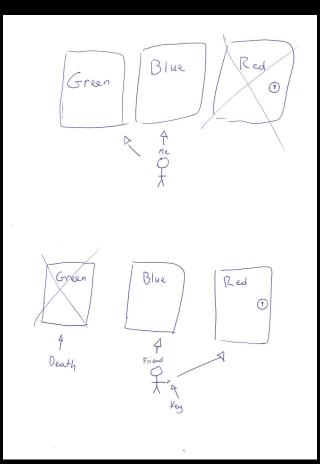


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Abstract away from irrelevant details: corridor, vase with the key, parrots, . . .



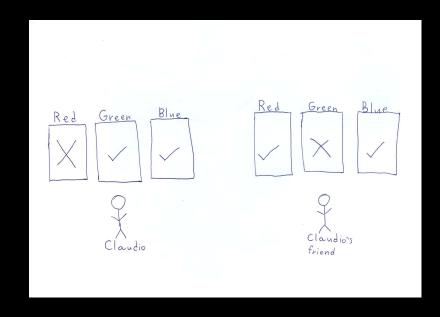
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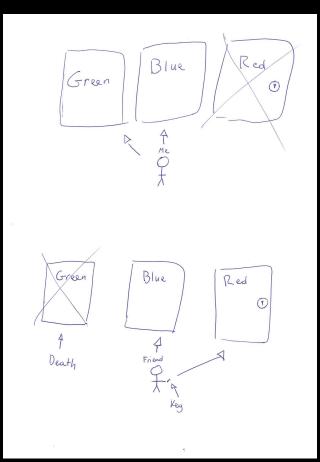
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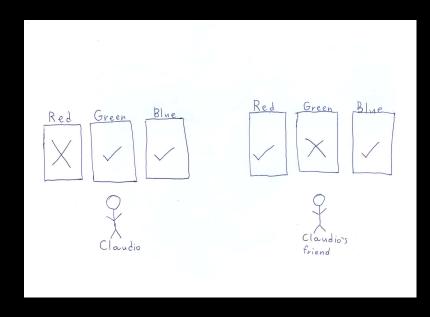
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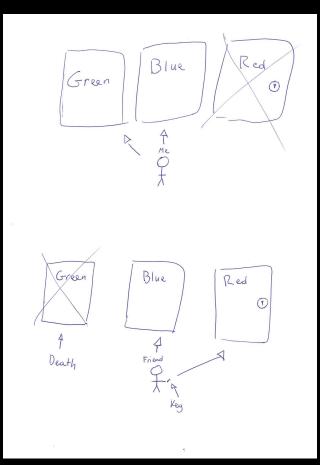
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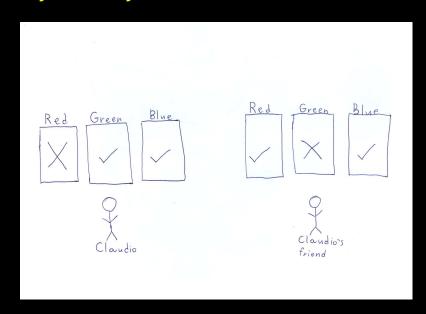


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# Modelling Behaviour

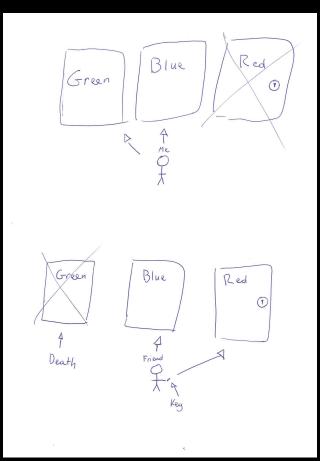
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— state —



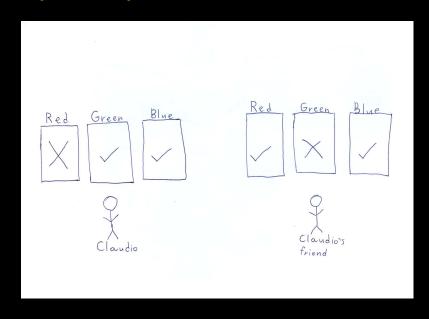
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Red Blue Green Green Blue Red

Claudio (9 year old)

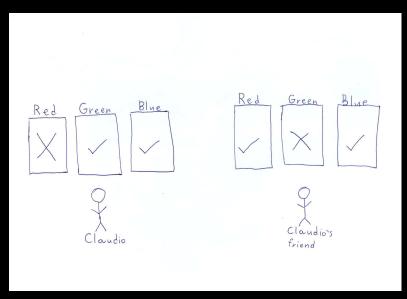
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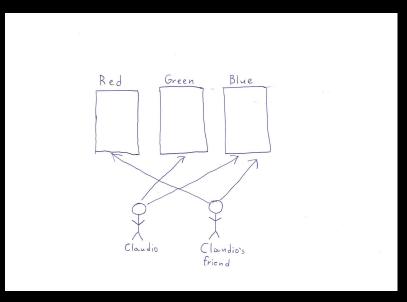
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How to compose the two parallel behaviours?

# Composing Behaviours





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The parrot on the left also tells you that your friends knows

- which between the green and the blue door will certainly lead to death, and
- that what you know contains the additional information your friend needs in order to be sure to safely reach the treasure.

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  - your friend has not arrived at the castle yet and you wait for her/him but he/she may refuse to collaborate with you.
  - your friend has already gone through when you arrive at the castle
     you will wait forever (starvation)

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- Otherwise independent action may lead to better (entire treasure) but uncertain results (treasure already taken or even death)
- Uncertainty may not be due to randomness but, instead, to time issues (real-time and time-critical systems)

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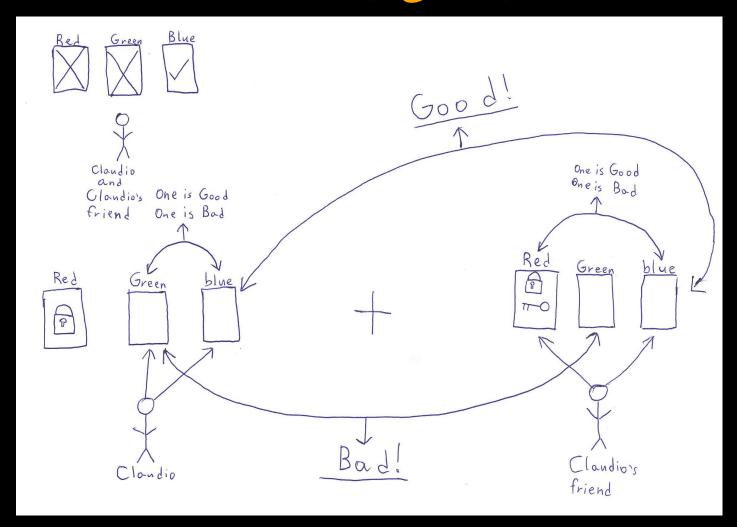
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Misunderstanding: we do not expect a child to appreciate these concepts, but to be exposed to them in a context with which the child is familiar with (a story) and, possibly, to internalise them.

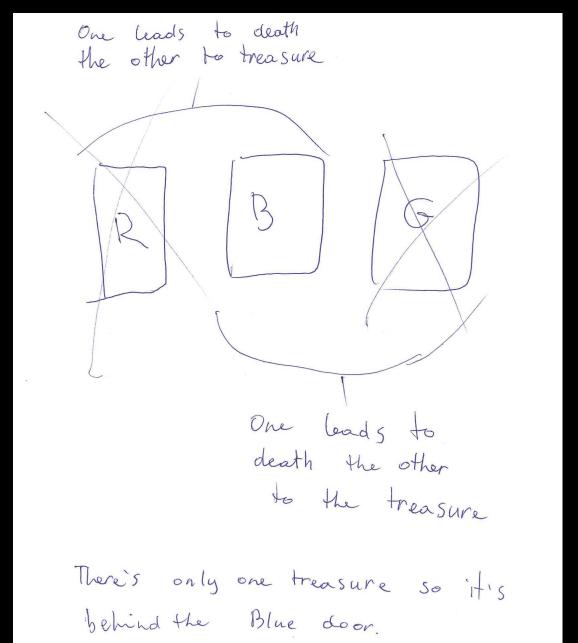
# Correctness Proof (age 9)

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There is no case study here. And there are no result This is a position paper

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An unplugged, problem-based approach can successfully work to expose children to concurrency concept.

- almost no technical jargon is introduced with the children (apart from some colourful jargon like "starvation")
- a single example of story is used to explore a large variety of concepts through the paper just for illustrative purposes.